

Mark schemes

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# Contents

| Introduction                | 5  |
|-----------------------------|----|
| General guidance            | 5  |
| Mark scheme for paper 1     | 12 |
| Mark scheme for paper 2     | 18 |
| Level threshold information | 25 |

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# Introduction

This booklet contains the mark schemes for papers 1 and 2 of the Optional level 6 tests in mathematics.

Each mark scheme was devised after trialling the tests with pupils and contains examples of some frequently occurring correct and incorrect answers given in the trials. Each mark scheme indicates the criteria against which judgements should be made.

The last section of this booklet provides information about interpreting the scores from the tests.

#### General guidance

#### The structure of the mark schemes

The marking information for each question is set out in the form of tables, which start on page 12 of this booklet. The ' $\mathbf{Q}$ ' column on the left-hand side of each table provides a quick reference to the question number. The '**mark**' column indicates the total number of marks available for each question part.

On some occasions the symbol  $(u_1)$  may be shown in the mark column. The 'U' indicates that there is a *Using and applying mathematics* element in the question. The number, 1, shows the number of marks attributed to using and applying mathematics in this question.

The '**correct response**' column may include two types of information:

- a statement of the requirements for the award of each mark, with an indication of whether credit can be given for correct working
- examples of some different types of correct response.

The '**additional guidance**' column indicates alternative acceptable responses, and provides details of specific types of response which are unacceptable. Other guidance, such as the range of acceptable answers, or when 'follow-through' is allowed, is provided as necessary.

#### Applying the mark schemes

In order to ensure consistency of marking, the most frequent procedural queries are listed on pages 6 and 7 along with the action the marker will take. This is followed by further guidance relating to the marking of questions that involve money, time and other measures, coordinates, probability and algebra. Unless otherwise specified in the mark scheme, markers should apply the following guidelines in all cases.

| Marking procedure   |  |  |
|---|--|--|
| Markers should award the mark unless the mark scheme states otherwise.  |  |  |
| Markers should use their judgement in deciding whether the response<br>corresponds with the statement of the requirements given in the 'correct<br>response' column. Reference will also be made to the 'additional guidance'<br>and, if there is still uncertainty, markers should consult the supervising marker.   |  |  |
| Calculations, formulae and written responses do not have to be set out in<br>any particular format. Pupils may provide evidence in any form as long as its<br>meaning can be understood. Diagrams, symbols or words are acceptable for<br>explanations or for indicating a response. Any correct method of setting out<br>working, however idiosyncratic, should be accepted. Provided there is no<br>ambiguity, condone the continental practice of using a comma for a<br>decimal point.  |  |  |
| This is when the pupil misreads the information given in the question and uses different information without altering the original intention or difficulty level of the question. For each misread that occurs, deduct one mark only.   |  |  |
| Where a pupil has shown understanding of the question, the mark(s) should be<br>given. In particular, where a word or number response is expected, a pupil may<br>meet the requirement by annotating a graph or labelling a diagram elsewhere<br>in the question.   |  |  |
| <ul> <li>Where appropriate, detailed guidance will be given in the mark scheme, which markers should follow. If no guidance is given, markers will need to examine each case to decide whether:</li> <li>the incorrect answer is due to a transcription error</li> <li>in questions not testing accuracy, the correct answer has been given but then rounded or truncated</li> <li>the pupil has continued to give redundant extra working which does not contradict work already done</li> <li>the pupil has continued to give redundant extra working which does contradict work already done.</li> </ul> | If so, the mark should be awarded.<br>If so, the mark should not be awarded.<br>Where a question part covers more<br>than one mark, only the final mark<br>should be withheld.   |  |
|   | <ul> <li>Marking procedure</li> <li>Markers should award the mark unless the Markers should use their judgement in decorresponds with the statement of the reresponse' column. Reference will also be and, if there is still uncertainty, markers sheed and, if there is still uncertainty, markers sheed and, if there is still uncertainty, markers sheed and particular format. Pupils may provide meaning can be understood. Diagrams, sexplanations or for indicating a response working, however idiosyncratic, should be ambiguity, condone the continental prace decimal point.</li> <li>This is when the pupil misreads the inform different information without altering the the question. For each misread that occur Where a pupil has shown understanding given. In particular, where a word or num meet the requirement by annotating a gr in the question.</li> <li>Where appropriate, detailed guidance will be given in the mark scheme, which markers should follow. If no guidance is given, markers will need to examine each case to decide whether:</li> <li>the incorrect answer is due to a transcription error</li> <li>in questions not testing accuracy, the correct answer has been given but then rounded or truncated</li> <li>the pupil has continued to give redundant extra working which does not contradict work already done.</li> <li>the pupil has continued to give redundant extra working which does contradict work already done.</li> </ul> |  |

| What if   | Marking procedure  |  |  |  |
|---|--|--|--|--|
| The pupil's answer is<br>correct but the wrong<br>working is shown.   | A correct response should always be marked as correct unless the mark scheme states otherwise.   |  |  |  |
| The pupil has made a conceptual error.  | In some questions, a method mark is available provided the pupil has made<br>a computational, rather than conceptual, error. A computational error is a<br>'slip' such as writing $4 \times 6 = 18$ in an otherwise correct long multiplication.<br>A conceptual error is a more serious misunderstanding of the relevant<br>mathematics; when such an error is seen no method marks may be awarded.<br>Examples of conceptual errors are: |  |  |  |
|   | - misunderstanding of place value, such as multiplying by 2 rather than 20 when calculating $35 \times 27$   |  |  |  |
|   | <ul> <li>subtracting the smaller value from the larger in calculations such as</li> <li>45 – 26 to give the answer 21</li> </ul>   |  |  |  |
|   | <ul> <li>incorrect signs when working with negative numbers.</li> </ul>  |  |  |  |
| The correct response<br>has been crossed out<br>and not replaced.   | Any legible crossed-out work that has not been replaced should be marked according to the mark scheme. If the work is replaced, then crossed-out work should not be considered.  |  |  |  |
| More than one answer<br>is given.   | If all answers are correct (or a range of answers is given, all of which are correct), the mark should be awarded unless prohibited by the mark scheme.<br>If both correct and incorrect responses are given, no mark should be awarded.   |  |  |  |
| The pupil's answer<br>correctly follows<br>through from earlier<br>incorrect work.                                | Follow-through marks may be awarded only when specifically stated in the<br>mark scheme, but should not be allowed if the difficulty level of the question<br>has been lowered. Either the correct response or an acceptable follow-through<br>response should be marked as correct.   |  |  |  |
| The answer is correct<br>but, in a later part of<br>the question, the pupil<br>has contradicted this<br>response. | A mark given for one part should not be disallowed for working or answers given in a different part, unless the mark scheme specifically states otherwise.   |  |  |  |
| The pupil's accuracy is<br>marginal according to<br>the overlay provided.   | Overlays can never be 100% accurate. However, provided the answer is within, or touches, the boundaries given, the mark(s) should be awarded.  |  |  |  |
| The pupil has drawn<br>lines which do not<br>meet at the correct<br>point.  | Markers should interpret the phrase 'slight inaccuracies in drawing' to mean<br>'within or on a circle of radius 2mm with centre at the correct point'.  |  |  |  |

## Marking specific types of question

#### Responses involving money

|  | Accept   | Do not accept  |
|--|--|--|
| Where the f sign<br>is given<br>for example: f3.20, f7<br>f  | f3.20<br>f7<br>f7.00<br>Any unambiguous indication of the correct<br>amount, eg<br>f3.20p<br>f3.20 pence<br>f3.20<br>f3.20<br>f3.20<br>f3.20<br>f3.20<br>f3.20<br>f3.20<br>f3.20 | Incorrect placement of pounds or pence, eg<br>f320<br>f320p<br>Incorrect placement of decimal point,<br>or incorrect use or omission of 0, eg<br>f3.2<br>f3 200<br>f32 0<br>f3-2-0 |
| Where the p sign<br>is given<br>for example: 40p<br><b>p</b> | 40p<br>Any unambiguous indication of the correct<br>amount, eg<br>f0.40p<br>f.40p<br>f0.40 with p sign crossed out   | Incorrect or ambiguous use of pounds<br>or pence, eg<br>0.40p<br>£40p  |
| Where no sign<br>is given<br>for example:<br>£3.20, 40p      | £3.20<br>320p<br>40p<br>£0.40<br>£3.20p<br>Any unambiguous indication of the correct<br>amount in £ or p as shown above  | Omission of final zero, eg<br>3.2<br>0.4   |

#### Responses involving time

|                       | Accept                                     | Do not accept                                  |
|-----------------------|--|--|
| A time interval       | 2 hours 30 minutes                         |  |
| for example:          | Any unambiguous, correct indication, eg    | Incorrect or ambiguous time interval, eg       |
| 2 hours 30 minutes    | $2\frac{1}{2}$ hours                       | 2.3 hours                                      |
| 2 110413 00 111114163 | 2.5 hours                                  | 2.3h   |
|                       | 2h 30                                      | 2h 3   |
|                       | 2h 30 min                                  | 2.30 min                                       |
|                       | 2 30                                       | 2.30   |
|                       | Digital electronic time, ie                | 2-30   |
|                       | 2:30                                       | 2,30   |
|                       |  | 2.3  |
| A specific time       | 8:40am                                     |  |
| for example:          | 8:40                                       |  |
| 9:40pm 17:20          | twenty to nine                             |  |
| 0.40dm, 17.20         | Any unambiguous, correct indication, eg    | Incorrect time, eg                             |
|                       | 08.40                                      | 8.4am  |
|                       | 8.40                                       | 8.40pm   |
|                       | 0840                                       | Incorrect placement of separators, spaces, etc |
|                       | 8 40                                       | or incorrect use or omission of 0, eg          |
|                       | 8-40                                       | 840  |
|                       | 8,40                                       | 8:4:0  |
|                       | Unambiguous change to 12 or 24 hour clock, | 8.4  |
|                       | eg   | 084  |
|                       | 17:20 as 5:20pm or 17:20pm                 | 84   |

#### **Responses involving measures**

|   | Accept  | Do not accept                                     |
|---|---|---|
| Where units<br>are given<br>(eg kg, m, l)<br>for example: 8.6kg | 8.6kg<br>Any unambiguous indication of the correct<br>measurement, eg<br>8.60kg<br>8.6000kg | Incorrect or ambiguous use of units, eg<br>8600kg |
| kg  | 8.6000kg<br>8kg 600g  |   |

#### Note

If a pupil leaves the answer box empty but writes the answer elsewhere on the page, then that answer must be consistent with the units given in the answer box and the conditions listed above.

If a pupil changes the unit given in the answer box, then their answer must be equivalent to the correct answer using the unit they have chosen, unless otherwise indicated in the mark scheme.

#### Responses involving coordinates

|              | Accept                      | Do not accept                       |
|--------------|-----------------------------|-------------------------------------|
| For example: | Unconventional notation, eg | Incorrect or ambiguous notation, eg |
| (5, 7)       | (05, 07)                    | (7, 5)                              |
|              | (five, seven)               | <i>y x</i><br>(7, 5)                |
|              | x y<br>(5, 7)               | (5x, 7y)                            |
|              | (x=5, y=7)                  | $(5^{x}, 7^{y})$<br>(x-5, y-7)      |

#### Responses involving probability

|   | Accept   | Take care! Do not accept ×   |  |
|---|--|--|--|
| A numerical probability<br>should be expressed as<br>a decimal, fraction or<br>percentage only.<br>For example:<br>0.7 $\frac{7}{10}$ 70% | Equivalent decimals, fractions and percentages,<br>eg<br>0.700<br>$\frac{70}{100}$<br>$\frac{35}{50}$<br>70.0%   | The first <b>four</b> categories of error below shou<br>be ignored if accompanied by an acceptable<br>response, but should not be accepted on<br>their own.<br>However, to avoid penalising the first <b>three</b><br>types of error below more than once within<br>each question, do not award the mark for<br>the <i>first</i> occurrence of each type of error<br>unaccompanied by an acceptable response.<br>Where a question part carries more than one<br>mark, only the final mark should be withheld |  |
|   | A probability correctly expressed in one<br>acceptable form which is then incorrectly<br>converted, but is still less than 1 and greater<br>than 0, eg<br>$\frac{70}{100} = \frac{18}{25}$ | <ul> <li>! A probability that is incorrectly expressed, eg 7 in 10 7 over 10 7 out of 10 7 from 10</li> <li>! A probability expressed as a percentage without a percentage sign.</li> <li>! A fraction with other than integers in the numerator and/or denominator.</li> <li>! A probability expressed as a ratio, eg 7:10, 7:3, 7 to 10</li> <li>* A probability greater than 1 or less than 0</li> </ul>  |  |

#### Responses involving the use of algebra

|   | Accept   | Take care! Do not accept ×   |
|---|--|--|
| For example:<br>2 + n<br>n + 2<br>2n<br>$\frac{n}{2}$<br>n <sup>2</sup> | Unambiguous use of a different case or<br>variable, eg<br><i>N</i> used for <i>n</i><br><i>x</i> used for <i>n</i>     | <ul> <li>! Unconventional notation, eg</li> <li>n × 2, or 2 × n, or n2</li> <li>or n + n for 2n</li> <li>n × n for n<sup>2</sup></li> <li>n ÷ 2 for n/2 or 1/2 n</li> <li>2 + 1n for 2 + n</li> <li>2 + 0n for 2</li> <li>Within a question that demands simplification, do not accept as part of a final answer involving algebra. Accept within a method when awarding partial credit, or within an explanation or general working.</li> <li>* Embedded values given when solving equations, eg</li> <li>in solving 3x + 2 = 32, 3 × 10 + 2 = 32 for x = 10</li> <li>To avoid penalising the two types of error below more than once within each question, do not award the mark for the first occurrence of each type within each question. Where a question carries more than one mark, only the final mark should be withheld.</li> </ul> |
|   | Words used to precede or follow equations or<br>expressions, eg<br>t = n + 2 tiles or tiles = $t = n + 2for t = n + 2$ | <ul> <li>Words or units used within equations or expressions, eg</li> <li>n tiles + 2</li> <li>n cm + 2</li> <li>Do not accept on their own. Ignore if accompanying an acceptable response.</li> </ul>   |
|   | Unambiguous letters used to indicate expressions, eg   | ✗ Ambiguous letters used to indicate expressions, eg   |
|   | t = n + 2  for  n + 2  | n = n + 2 for $n + 2$  |

| Q | Mark           | Correct response   |  |  |                             |                | Additional guidance                                      |
|---|----------------|--|--|--|-----------------------------|----------------|--|
| 1 | 2m             | Completes all 8 entries of the table correctly, ie   |  |  |                             |                |  |
|   |                |  | <b>do</b> wear<br>glasses  | <b>do not</b><br>wear glasses  | Total                       |                |  |
|   |                | boys   | 1  | 15   | 16                          |                |  |
|   |                | girls  | 3  | 11   | 14                          |                |  |
|   |                | Total  | 4  | 26   | 30                          |                |  |
|   | or<br>1m<br>U2 | Complete   | es at least fou  | ur entries corre   | ctly                        |                |  |
| 2 | 2m             | Indicates<br>A as (7, 13   | correct coord<br>3) and B as (1  | dinates for botl<br>7, 13)   | n points                    | , ie           |  |
|   | or<br>1m<br>U2 | Indicates correct coordinates for one point<br>or<br>Transposes the responses, ie<br>A as (17, 13) and B as (7, 13)<br>or<br>The only error is to indicate incorrect, but consistent,<br>y ordinates, provided $y > 3$<br>eg |  |  |                             |                |  |
| 3 | 2m<br>or<br>1m | 16<br>8<br>or<br>Answer of<br>(the only or<br>or<br>Shows un<br>there are<br>eg<br>• $\frac{2}{3} \times 24$   | f 17 with $\frac{50}{3}$<br>error is to fail<br>derstanding<br>computation<br>= 12 | or equivalent so<br>I to subtract 1 a<br>of a correct me<br>nal errors | een<br>at the st<br>ethod e | art)<br>ven if | × Answer of 17 without $\frac{50}{3}$ or equivalent seen |
| 4 | 1m             | 1 : 3  |  |  |                             |                |  |
|   | 1m             | 28%  |  |  |                             |                | * Equivalent fractions or decimals                       |

| Q | Mark     | Correct response   | Additional guidance      |
|---|----------|--|--------------------------|
| 5 | 2m       | Gives all three correct values, ie   |                          |
|   |          | <i>a</i> = 16, <i>b</i> = 8, <i>c</i> = 6  |                          |
|   | or<br>1m | Gives at least one correct value   |                          |
|   |          | <ul> <li>or</li> <li>Gives three values that satisfy the second and third equations</li> <li>eg</li> <li>a = 18, b = 6, c = 8 <ul> <li>(satisfies a + b = 24 and b + c = 14 : note that a - c = 10)</li> </ul> </li> </ul> |                          |
| 6 | 1m       | Indicates the correct area eg •  | ✓ Unambiguous indication |
|   | 1m       | Indicates the correct area eg •  | ✓ Unambiguous indication |

| 0 | Mark | Correct response   | Additional guidance   |
|---|------|--|---|
| 7 | 1m   | <ul> <li>Gives a correct description for B that shows or implies the link between the two variables</li> <li>eg</li> <li>The more computers a person has in their home, the fewer hours they are likely to spend watching television</li> <li>There is negative correlation between the number of hours watched and the number of computers in the home</li> <li>If you have lots of computers you don't tend to watch TV much</li> </ul>  | <ul> <li>Minimally acceptable description         eg         More computers, less watching         Fewer computers, more TV         More television, less computers         Less TV, more computers         Negative correlation         Mumber of hours watching interpreted         incorrectly as number of televisions         Condone         eg, for the first mark accept         The more computers people have, the fewer         TVs they have         Incomplete description</li> </ul>  |
|   | 1m   | <ul> <li>Gives a correct description for C that states or implies that the two variables are not linked</li> <li>eg</li> <li>How much television a person watches is independent of the number of mobile phones they have</li> <li>There is no correlation between the number of hours watched and the number of phones</li> <li>Time watching is not dependent on the amount of mobiles</li> <li>People with lots of mobile phones don't necessarily watch any more than those with just one</li> </ul> | <ul> <li>Incomplete description eg <ul> <li>If you have one computer you watch more TV</li> </ul> </li> <li>Minimally acceptable description eg <ul> <li>Mobiles don't affect watching</li> <li>No correlation</li> <li>Not connected</li> <li>No relationship</li> <li>No link</li> <li>No pattern</li> <li>It's random</li> <li>More or less phones won't affect hours</li> <li>Number of mobiles doesn't affect the situation</li> <li>Someone watching 1 hour of TV might have as many mobiles as someone who watches 8 hours [generality implied]</li> <li>How much is watched depends on the person not on their mobile phones</li> </ul> </li> </ul> |
|   |      |  | <ul> <li>Incomplete description         eg         <ul> <li>There is a range of numbers of mobile phones             and the number of hours spent watching TV</li> <li>It doesn't make much difference</li> </ul> </li> <li>Description of graph's appearance         Accept alongside a correct response         eg, for C accept         <ul> <li>It's all spread out so there is no link         eg, for C do not accept</li> <li>It's all spread out</li> </ul> </li> </ul>  |

| Q | Mark                         | Correct response  | Additional guidance   |
|---|------------------------------|---|---|
| 8 | Mark<br>1m<br>2m<br>or<br>1m | Correct response<br>Indicates No and gives a correct explanation<br>eg<br>• The angles are not the same size<br>• A regular pentagon looks like this,<br>with its angles all the same size<br>• All the angles should be 108°<br>• It doesn't have rotation symmetry<br>• It's got more sides than a square so all its angles<br>should be obtuse, but they're not<br>• It's got more sides than a square so all its angles<br>should be obtuse, but they're not<br>• Of<br>• Of<br>• Shows that the 150° angle can be split into | <ul> <li>✓ Minimally acceptable explanation eg <ul> <li>90 ≠ 150</li> <li>Different angles</li> <li>A regular pentagon doesn't have right angles in it</li> <li>A regular one can't have 150° angles</li> <li>It doesn't look the same when it's turned</li> <li>Not all the angles are obtuse</li> </ul> </li> <li>Incorrect angle size for a regular pentagon given Condone alongside a correct response eg, accept <ul> <li>The angles are different, they should be 60° (error, but all equal implied)</li> <li>The angles should all be 70° (error) eg, do not accept <ul> <li>The 90° angles should be 60° (does not imply the angles should all be the same)</li> </ul> </li> <li>X Incomplete explanation eg <ul> <li>Not the same</li> <li>It has two right angles</li> <li>Two angles are the same</li> <li>A regular pentagon looks like this</li> <li>A regular pentagon looks like this wertical lines</li> </ul> </li> <li>Indicates Yes, or no decision made, but explanation clearly correct Condone provided the explanation is more than minimal</li> </ul></li></ul> |
|   |                              | 90° and 60°<br>or<br>Divides the pentagon vertically and shows that<br>half <i>a</i> is 30°<br>or<br>Draws triangles to show a rectangle, labelling the<br>non-right angles on at least one side correctly<br>eg<br>• $60^{\circ}$<br>$30^{\circ}$<br>or<br>Shows or implies that the angle sum of a pentagon<br>is 540°  |   |

| Q  | Mark     | Correct response   | Additional guidance   |
|----|----------|--|---|
| 9  | 1m       | Indicates D  |   |
|    |          | then   |   |
|    |          | Indicates B  |   |
|    | 1m       | Gives a correct equation   | ✓ Line not drawn or incorrect   |
|    |          | eg<br>• $y = 4$<br>• $y - 4 = 0$   | × Follow-through from their incorrect line                                  |
| 10 | 1m       | Joins dots to make a triangle that has only one side of 4cm and only one angle of 45°. | ! Lengths or angles shown on their triangle(s)<br>Ignore, even if incorrect |
|    | U1       |  | × Dots not used   |
| 11 | 1m       | 16   |   |
|    | 1m       | 800  |   |
| 12 | 1m       | Gives four numbers that sum to 16 and have a range                                     | <ul> <li>✓ Numbers given in any order</li> </ul>                            |
|    |          |  | • 3, 7, 3, 3  |
|    |          | 1, 5, 5, 5<br>or   | ✓ Decimals or fractions used  |
|    |          | 2, 2, 6, 6<br>or   | eg<br>• 1.5. 4. 5. 5.5  |
|    |          | 2, 3, 5, 6   | -, -, -,  |
|    | $\frown$ | or<br>2, 4, 4, 6   |   |
|    |          | or<br>3, 3, 3, 7   |   |

| Q  | Mark       | Correct response   | Additional guidance   |
|----|------------|--|---|
| 13 | 1m<br>(U1) | 19   |   |
| 14 | 1m         | <ul> <li>Indicates the answer could be positive or negative and gives a correct explanation</li> <li>eg</li> <li>A positive multiplied by -5 gives a negative answer, but a negative multiplied by -5 gives a positive answer</li> <li>Positive numbers will become negative, negative numbers will become positive</li> <li>If the number is 10 the answer will be -50, which is negative, but if the number is -10, the answer is 50, ie positive</li> </ul> | <ul> <li>✓ Minimally acceptable explanation         <ul> <li>eg</li> <li>10 becomes negative, but -10 becomes             positive</li> <li>+ve → -ve             -ve → +ve</li> <li>-5 × -3 = 15, -5 × 3 = -15</li> </ul> </li> <li>✓ Incomplete explanation         eg         <ul> <li>-5 × 3 = -15</li> <li>The original number could be positive or             negative so the answer could be positive or             negative</li> </ul> </li> <li>Makes an incorrect decision, or no decision         made, but explanation clearly correct         Condone provided the explanation is more than         minimal</li> </ul> |

| Q | Mark           | Correct response   | Additional guidance   |
|---|----------------|--|---|
| 1 | 1m             | Shows the correct rotation, ie   | <b>! Lines not ruled or accurate</b><br>Accept slight inaccuracies in drawing<br>(see general guidance)   |
| 2 | 1m             | 20   |   |
|   | 1m<br>(U1)     | 33.125   | <ul> <li>✓ Equivalent fractions or decimals</li> </ul>  |
| 3 | 2m<br>or<br>1m | Completes all three rows correctly, ie   |   |
| 4 | 2m<br>or<br>1m | 26<br>Shows or implies a complete method with not more than one computational error or rounding error eg<br>• 35 x 24.75 = 860 (error)<br>1200 - 860 = 340<br>340 ÷ 12.5 = 27.2<br>Answer = 27<br>• (1200 - 35 x 24.75) ÷ 12.5<br>• 1200 - 866.25 = 333.75<br>333.75 ÷ 12.5<br>or<br>26.7 seen<br>or<br>Shows the correct total for the trees, ie<br>£1191.25<br>or<br>Shows the correct change, ie<br>£8.75 | <ul> <li>Answer of £26</li> <li>Answer of 27 without a correct method shown or implied</li> <li>Method used for ÷ 12.5 is repeated subtraction Do not accept as a correct method</li> </ul> |

| Q | Mark                 | Correct response  | Additional guidance  |
|---|----------------------|---|--|
| 5 | 1m<br>(U1)           | <ul> <li>Indicates Nik and gives a correct explanation eg</li> <li>1 sandwich, 2 apples and 1 banana is missing from the graph and that is what Nik had in his lunch box</li> <li>The graph shows the correct number of fruit bars and Nik is the only one who does not have a fruit bar in his lunch box so his must be the missing one</li> <li>The totals from the table are 7, 6, 5, 6, and from the graph 6, 4, 4, 6, and the difference is Nik</li> </ul> | <ul> <li>Minimally acceptable explanation         eg         <ul> <li>1 sandwich, 2 apples, 1 banana</li> <li>Because the number of fruit bars is correct</li> <li>1 banana missing</li> <li>7, 6, 5, 6 and 6, 4, 4, 6 seen</li> </ul> </li> <li>Incorrect or incomplete explanation         eg         <ul> <li>1 sandwich, 2 apples</li> <li>There are 6 fruit bars</li> <li>2 apples are missing</li> </ul> </li> </ul> |
| 6 | 3m<br>or<br>2m<br>or | Completes the drawing according to the following conditions, with a tolerance of 3mm in each case the circle has a diameter of 8cm the highest point at which the circle crosses the central vertical line is 3cm from the top of the answer box the lowest point at which the circle crosses the central vertical line is 7cm from the bottom of the answer box $\int \frac{3cm}{7cm} \sqrt{7cm}$  | <ul> <li>Flag constructed 'upside down'</li> <li>Shading incorrect or omitted, or additional lines drawn<br/>Condone, provided the response is unambiguous</li> <li>Compasses not used<br/>For pupils who meet one or more of the conditions without using compasses, deduct<br/>ONE mark</li> </ul>   |
|   | 1m                   | Any one of the three conditions given above is correct  |  |

| 7 3m $13\frac{1}{2}$ or equivalent<br>or<br>2m Shows or implies a complete correct method with not<br>more than one computational error<br>The most common correct methods:<br>Find the total area of the trapezia and divide by 8<br>eg<br>• $(12^2 - 6^2) \div 8$<br>• $144 - 36 = 94$ (error)<br>$94 \div 8 = 11.75$<br>Find the dimensions of a trapezium and use the<br>formula or component parts<br>eg<br>• $\frac{1}{2}(3 + 6) \times 3$<br>• $4\frac{1}{2} \times 3$<br>• $3 \times 3 + (3 \times 3) \div 2$<br>or  | uidance  | k Correct response   | Q |
|--|--|--|---|
| or<br>2mShows or implies a complete correct method with not<br>more than one computational error $\times$ Squaring evaluated as $\times 2$<br>eg<br>• $(12^2 - 6^2) \div 8$<br>• $144 - 36 = 94$ (error)<br>$94 \div 8 = 11.75$ $\times$ Squaring evaluated as $\times 2$<br>eg<br>• $(12^2 - 6^2) \div 8$<br>• $(12^2 - 6^2) \div 8 = (24 - 12) \div 8$ Find the dimensions of a trapezium and use the<br>formula or component parts<br>eg<br>• $\frac{1}{2}(3 + 6) \times 3$<br>• $3 \times 3 + (3 \times 3) \div 2$ $\times$ Squaring evaluated as $\times 2$<br>eg<br>• $(12^2 - 6^2) \div 8 = (24 - 12) \div 8$ |  | 13 $\frac{1}{2}$ or equivalent   | 7 |
|  | g evaluated as $\times$ 2<br>$6^2$ ) ÷ 8 = (24 – 12) ÷ 8 | Shows or implies a complete correct method with not<br>more than one computational error<br>The most common correct methods:<br>Find the total area of the trapezia and divide by 8<br>eg<br>• $(12^2 - 6^2) \div 8$<br>• $144 - 36 = 94$ (error)<br>$94 \div 8 = 11.75$<br>Find the dimensions of a trapezium and use the<br>formula or component parts<br>eg<br>• $\frac{1}{2}(3+6) \times 3$<br>• $4\frac{1}{2} \times 3$<br>• $3 \times 3 + (3 \times 3) \div 2$<br>or |   |
| The only error is to work with 4 congruent trapezia<br>(not 8), but correctly finds the area of one of them<br>eg<br>• $(144 - 36) \div 4 = 27$<br>•<br>•<br>•<br>•<br>•<br>•<br>•<br>•<br>•<br>•<br>•<br>•<br>•<br>•<br>•<br>•<br>•<br>•<br>•   | 27 seen with no method                                   | The only error is to work with 4 congruent trapezia<br>(not 8), but correctly finds the area of one of them<br>eg<br>• $(144 - 36) \div 4 = 27$<br>•<br>•<br>•<br>•<br>•<br>•<br>•<br>•<br>•<br>•<br>•<br>•<br>•<br>•<br>•<br>•<br>•<br>•<br>•   |   |
| area of the trapezia<br>eg<br>• $(12^2 - 6^2)$<br>• $144 - 36$<br>• $108$ seen<br>or<br>Show the parallel sides of the trapezium are 3(cm)<br>and 6(cm), and the height is 3(cm)<br>eg<br>• Diagram marked correctly   | condone<br>pt<br>6 <sup>2</sup> ÷ 8 = 139.5              | <ul> <li>area of the trapezia</li> <li>eg</li> <li>(12<sup>2</sup> - 6<sup>2</sup>)</li> <li>144 - 36</li> <li>108 seen</li> <li>or</li> <li>Show the parallel sides of the trapezium are 3(cm) and 6(cm), and the height is 3(cm)</li> <li>eg</li> <li>Diagram marked correctly</li> </ul>  |   |

| Q | Mark | Correct response Additional guidance  |
|---|------|---------------------------------------|
| 8 | 1m   | The first 3 multiples of 10 add to 60 |
|   | 1m   | The first 4 multiples of 6 add to 60  |
|   |      | The first 2 multiples of 20 add to 60 |
|   | U1   | The first 1 multiples of 60 add to 60 |

| Q | Mark     | Correct response   | Additional guidance                              |
|---|----------|--|--|
| 9 | 2m       | 16.8p or 17p or equivalent   | <b>! Money</b><br>See general guidance on page 8 |
|   | or<br>1m | Shows the digits 168 or 17   |  |
|   |          | or   |  |
|   |          | Shows a complete correct method with not more than one computational or rounding error |  |
|   |          | eg<br>• $56 \times 10 \times 3 \div 100$<br>• $56(0) \times 0.03$                      |  |
|   |          | <ul> <li>560 ÷ 100 = 5.6</li> <li>6p (premature rounding) × 3 = 18</li> </ul>          |  |

| Q  | Mark | Correct response   | Additional guidance   |
|----|------|--|---|
| 10 | 1m   | <ul> <li>Gives correct information for x = 4</li> <li>eg</li> <li>4, too big</li> <li>4, too high</li> <li>4, too much above 1</li> </ul>  | <ul> <li>Incomplete information that does not link to<br/>the value of 1<br/>eg</li> <li>4, too incorrect</li> </ul>  |
|    | 1m   | Gives correct information for <i>x</i> = 3.5 eg<br>• 1.75, too big   | <ul> <li>In both the first and second answers, shows correct values but omits or gives incorrect further information</li> <li>eg <ul> <li>4, too small</li> <li>1.75, too</li> </ul> </li> <li>Do not award the first mark, but award the second mark</li> </ul> <li>Value rounded <ul> <li>Accept 1.8</li> <li>Do not accept 1.7</li> </ul></li>   |
|    | 1m   | Gives a logical value for the next trial, and justifies<br>their decision<br>eg<br>• 3.2, because I know it is between 3 and 3.5<br>• 3.25, it is halfway between 3 and 3 and a half<br>• 3.3 because it is bigger than 3 which was too small<br>but smaller than 3.5 which was too big<br>• 3.4, it has to be smaller than 3.5 (that it is greater<br>than 3 is implicit) | <ul> <li>! Logical values <ul> <li>Accept any of the following: <ul> <li>3.1</li> <li>3.2</li> <li>3.3</li> <li>3.4</li> <li>3.25</li> </ul> </li> <li>Also accept any value between 3.3 and 3.4 provided their justification shows why the solution is between these values eg, accept (since a further trial has clearly taken place) <ul> <li>3.35, 3.3 is too small</li> <li>3.302, because 3.303 is just over 1 eg, do not accept</li> <li>3.35, because I know it is between 3 and 3.5</li> </ul> </li> <li>✓ Minimally acceptable justification eg <ul> <li>3.2, 3.5 is too big</li> </ul> </li> <li>× Incomplete justification eg <ul> <li>3.2, because it is at an appropriate interval</li> </ul> </li> <li>For the third part, follow-through <ul> <li>If their calculation in the second part for x = 3.5 was too small, accept x = 3.6, 3.7, 3.75, 3.8 or 3.9 alongside an explanation comparable with those given in the mark scheme</li> </ul> </li> </ul></li></ul> |

| Q  | Mark       | Correct response  | Additional guidance  |
|----|------------|---|--|
| 11 | 1m         | 105 ± 1<br>then<br>80 ± 1   |  |
|    | 1m<br>(U1) | 150 ± 1   |  |
| 12 | _          | Describes the key features of the information<br><b>2m</b> are available, one from each of the categories<br>A and B below:   |  |
|    | 1m         | <ul> <li>Category A</li> <li>States that the rate the mass of the dog increases slows as it gets older</li> <li>eg</li> <li>They get heavier in their first few months but as they get older their weight doesn't go up as much</li> </ul>            | <ul> <li>Minimally acceptable explanation         eg, for category A</li> <li>Grows quickly then more slowly</li> <li>After a few months the amount it increases         by gets smaller [accept any value from 4–8         months inclusive within this type of response]</li> <li>They start by gaining about 5kg per month</li> </ul>   |
|    | 1m         | <ul> <li>Category B</li> <li>Makes an observation that links the information in the bar chart to the adult mass</li> <li>eg</li> <li>It reaches adult size after the first year</li> <li>A dog is about half grown when it is 4 months old</li> </ul> | <ul> <li>but this gets less and less</li> <li>eg, for category B</li> <li>Doesn't get any fatter after it is a year old</li> <li>They stop at 12 months</li> <li>At 6 months, it's more than half-sized</li> <li>eg, for both categories (ie 2m)</li> <li>It grows quickly then slowly until 12 months when it stops</li> </ul>  |
|    |            |   | <ul> <li><b>Values given</b> As this question is assessing understanding of information presented graphically, condone incorrect numbers for category A, but do not accept for category B eg, for category A, accept <ul> <li>They increase by about 10kg per month but not as much as they get older</li> <li>eg, for category B, do not accept</li> <li>A dog is about half grown after half a year</li> </ul></li></ul> |
|    |            |   | <ul> <li>Incomplete explanation         eg, for category A</li> <li>Dogs get heavier as they get older [doesn't         say how rate of change alters]         eg, for category B</li> <li>A German Shepherd stops growing when it</li> </ul>  |

- reaches 35kg [no link to 12 months] • It grows quickly then slowly until 12 months [gains category A mark but no link to full
- weight being reached for category B]

# Level threshold information

This section provides information about interpreting the scores from the Optonal level 6 tests in mathematics.

In order to make use of the information in this section, you should administer the tests according to the guidance given in the test administrators' guide. The guide can be downloaded from the NCA Tools website at: <u>www.qcda.gov.uk/ncatools</u>. It is particularly important that you observe the time limits given in the test instructions, and mark questions strictly according to the mark scheme. If not, the information derived from this section cannot be used reliably.

The table below gives an indication of the national curriculum level for pupils, based on their score in the test. In order to use this information, the total scores on paper 1 and paper 2 should be added together.

#### Mathematics test (maximum mark 50)

| Score         | Outcome              |
|---------------|----------------------|
| 0 - 24 marks  | Level 6 not achieved |
| 25 - 50 marks | Level 6 achieved     |

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#### QCDA/11/5454

Optional level 6 tests | Mathematics mark schemes